Appendix M to:

A Theoretical Investigation to the Physical Constraints for Light Velocity in Empty Euclidian Space and first Consequences for Long-distance Physics.

Referred equations: (29), (31), (34)

Derivation of the function $\Theta()$ for force-free moving system transformation

Equation (29):

(29)
$$\frac{1}{\Theta(T_{\text{or}}, v_{\text{or}}; d_x, 0)} \frac{\partial \Theta}{\partial x}(T_{\text{or}}, v_{\text{or}}; d_x, 0) = -\frac{d_x + v(T_x(d_x)) T_x(d_x)}{\gamma^2 - d_x \{ d_x + v(T_x(d_x)) T_x(d_x) \}}$$

is general for any moving system but will be worked out specifically for the situation of a force-free movement; adapted from equation (34):

$$(M.1) \qquad d_x = d(T_x) = v_{or} T_{or} \left(1 - \frac{T_{or}}{T_x}\right)$$

and its first derivative:

(M.2)
$$v(T_x) = \left(\frac{d}{dT}d\right)(T_x) = v_{or} T_{or} \frac{T_{or}}{T_x^2}$$

It is easily seen that:

$$(M.3) \qquad d_x + v(T_x) T_x = v_{or} T_{or}$$

This result goes into equation (29):

(M.4)
$$\frac{1}{\Theta(T_{\rm or}, v_{\rm or}; d_{\rm x}, 0)} \frac{\partial \Theta}{\partial x}(T_{\rm or}, v_{\rm or}; d_{\rm x}, 0) = -\frac{v_{\rm or} T_{\rm or}}{\gamma^2 - d_{\rm x} v_{\rm or} T_{\rm or}}$$

which is straightforwardly solved as:

(31)
$$\Theta(T_{or}, v_{or}; d_x, 0) = \Theta(T_{or}, v_{or}; 0, 0) \left(1 - \frac{d_x v_{or} T_{or}}{\gamma^2}\right)$$